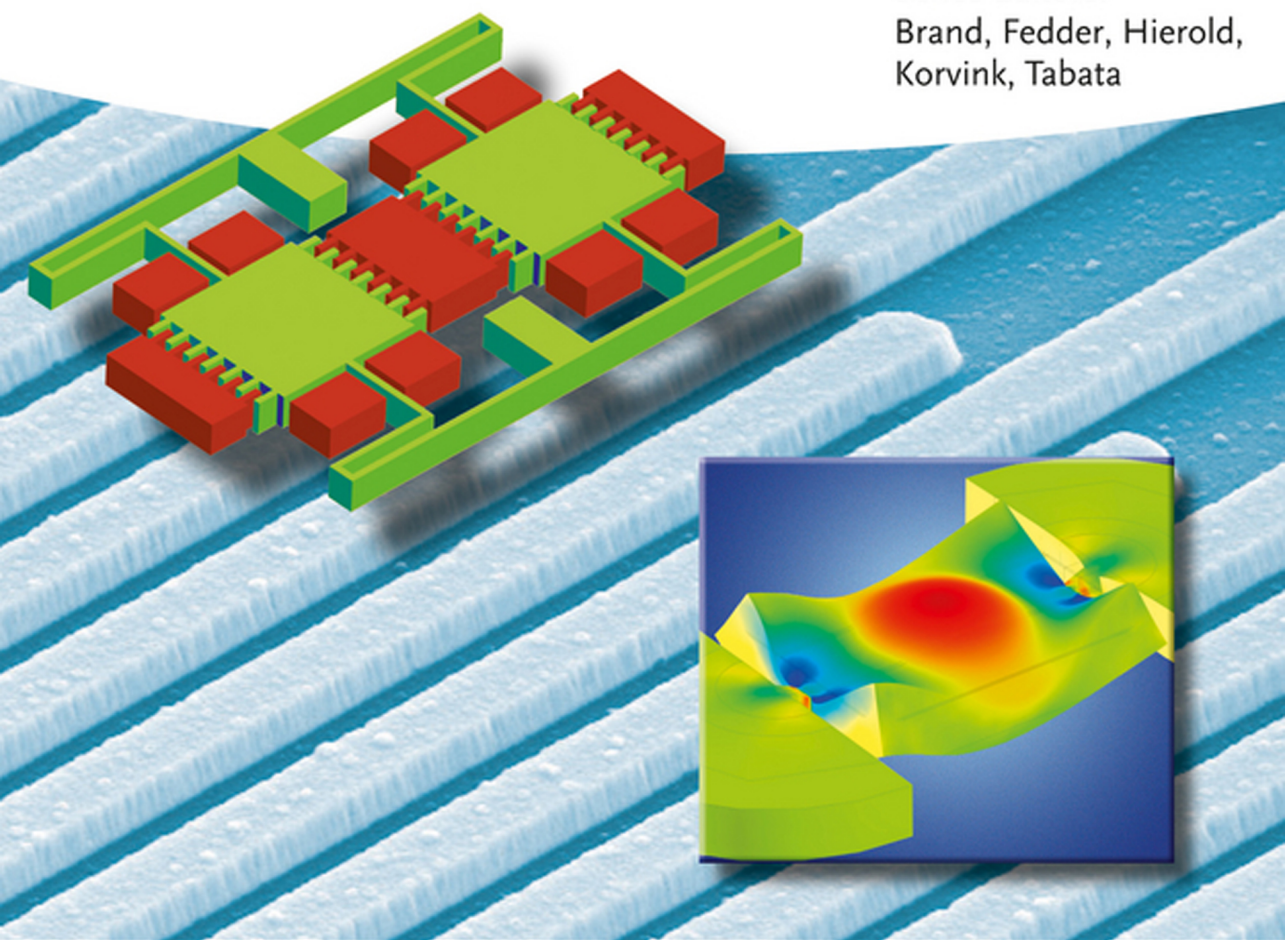


Oliver Brand, Isabelle Dufour, Stephen M. Heinrich,
Fabien Josse (Eds.)

Resonant MEMS

Fundamentals, Implementation
and Application

Series Editors:
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Korvink, Tabata



Edited by
Oliver Brand
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in electronic formats

*Edited by Oliver Brand, Isabelle Dufour, Stephen M. Heinrich,
and Fabien Josse*

Resonant MEMS

Fundamentals, Implementation and Application

WILEY-VCH
Verlag GmbH & Co. KGaA

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Library of Congress Card No.: applied for

British Library Cataloguing-in-Publication Data

A catalogue record for this book is available from the British Library.

Bibliographic information published by the Deutsche Nationalbibliothek

The Deutsche Nationalbibliothek lists this publication in the Deutsche Nationalbibliografie; detailed bibliographic data are available on the Internet at <<http://dnb.d-nb.de>>.

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Print ISBN: 978-3-527-33545-9

ePDF ISBN: 978-3-527-67636-1

ePub ISBN: 978-3-527-67635-4

Mobi ISBN: 978-3-527-67634-7

oBook ISBN: 978-3-527-67633-0

Cover Design Schulz

Typesetting Laserwords Private Limited, Chennai, India

Printing and Binding Markono Print Media Pte Ltd., Singapore

Printed on acid-free paper

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