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Jude Hemanth · Valentina Emilia Balas  
*Editors*

# Nature Inspired Optimization Techniques for Image Processing Applications

 Springer

# **Intelligent Systems Reference Library**

Volume 150

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Jude Hemanth · Valentina Emilia Balas  
Editors

# Nature Inspired Optimization Techniques for Image Processing Applications

 Springer

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ISSN 1868-4394

ISSN 1868-4408 (electronic)

Intelligent Systems Reference Library

ISBN 978-3-319-96001-2

ISBN 978-3-319-96002-9 (eBook)

<https://doi.org/10.1007/978-3-319-96002-9>

Library of Congress Control Number: 2018948603

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# Foreword

The active quest to endow machines with human abilities has been a feature of modern times. The ultimate goal of creating an artificially intelligent and autonomous entity has been approached through many intermediate steps by providing human-like functionality in a myriad of applications, including industrial automation, health care and security. A chief biological function that has been pursued is that of analysing and understanding visual information. Advances in image processing and computer vision have been adopted in a range of applications and have transformed what is possible to be done automatically and without the need for human visual intervention. In certain applications, machine capabilities have even surpassed what humans can do. However, while in some of these limited cases they have outstripped the human capabilities in terms of scale and speed, there are still areas where humans have the edge and, therefore, the search for better approaches and algorithms for image understanding continues.

At the same time, a better understanding of the emergence of biological systems, including humans, has drawn the designers of machine vision systems to try to learn from Nature. Through a very long process, spanning millennia, the Nature's own search for effective autonomous entities has resulted in efficient and effective mechanisms for understanding and interacting with the world. Scientists and designers are now learning from the fruits of Nature's long labour to expedite the development of artificial systems.

This volume brings together some of these naturally inspired approaches for image understanding in one place and also provides a sample of the vast array of applications to which they can be applied. For the reader new to these approaches, it will provide a good starting point and for the more advanced algorithm designers, it may suggest new ideas that they have not considered before.

The deep and vast experience of Nature is a great resource for engineers and designers in their quest for novel solutions to the current and emerging challenges that face humanity. It is hoped that this book will contribute to this quest and strengthens the case for the continued study of Nature in search of new insights.

Canterbury, UK  
August 2018

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# Preface

This edited book is one of the significant contributions in the field of intelligent systems for practical applications. This book is interdisciplinary with a wide coverage of topics from nature-inspired optimization techniques and image processing applications. The main objective of this book is to highlight the state-of-the-art methods in these interdisciplinary areas to the researchers and academicians. Variety of practical applications are covered in this book which can assist the budding researcher to choose his own area of research. This book also covers in-depth analysis of the methods which will attract high-end researchers to further explore or innovate in these areas. In a nutshell, this book is a complete product for usage by anyone working in the areas of intelligent systems. A brief introduction about each chapter is as follows.

Chapter 1 illustrates the application of firefly optimization algorithm for brain image analysis. Specifically, the methodology of CT and MRI brain image segmentation is analysed in detail. Chapter 2 deals with image compression using bat optimization techniques. An in-depth analysis of codebook generation for image compression is analysed which will attract the readers. Chapter 3 deals with natural language processing using particle swarm optimization methods. Few modified swarm approaches are suggested in this chapter for efficient categorization of alphabets in languages. The proposed approach is tested with Tamil language but can be extended to different languages across the globe.

Chapter 4 covers the application of grey wolf optimization algorithm for image steganography applications. Feature optimization for efficient data hiding is the main objective of the work covered in this chapter. Literature survey is one critical area of research which will attract several readers. With this idea, a detailed survey on nature-inspired techniques for image processing applications is dealt in Chap. 5. The application for ant colony optimization for visual cryptography is discussed in Chap. 6. The primary focus of this work is image enhancement which can assist in developing efficient cryptographic systems. Qualitative and quantitative analyses are covered in this chapter which is more beneficial to the readers.

The necessity of image analysis methods is significantly increasing in the area of agriculture. The application of swarm intelligence techniques for detecting the quality of crops via images is illustrated in Chap. 7. Analysing the quality of different stages of wheat is the main focus of this chapter. Chapter 8 discusses the various concepts of image preprocessing using cuckoo search optimization techniques. Different types of input images are used in this chapter to validate the proposed methodology. Automatic skin disease identification in mango fruits using artificial bee colony algorithm is the focus of Chap. 9. The optimization algorithm is used to select the optimal features for skin classification in this chapter.

Chapter 10 covers the different optimization techniques for fixing the structure of the complex deep convolutional neural networks. An efficient architecture will enhance the performance of any automated system. Chapter 11 deals with the application of differential evolution method for quality enhancement in underwater images. Chapter 12 covers the application of genetic algorithm for biometrics application. Fetal biometrics-based abnormality detection is the prime focus of this chapter.

We are grateful to the authors and reviewers for their excellent contributions for making this book possible.

Our special thanks go to Janus Kacprzyk and Lakhmi C. Jain (Series Editors to Intelligent Systems Reference Library) for the opportunity to organize this guest-edited volume.

We are grateful to Springer, especially to Dr. Thomas Ditzinger (Senior Editor) for the excellent collaboration.

We would like to express our gratitude and thanks to Handling Editor Ms. Rajalakshmi Narayanan, Springer, Chennai and her team for their wholehearted editorial support and assistance while preparing the manuscript.

This edited book covers the fundamental concepts and application areas in detail which is one of the main advantages of this book. Being an interdisciplinary book, we hope it will be useful to a wide variety of readers and will provide useful information to professors, researchers and graduated, and all will find this collection of papers inspiring, informative and useful.

Coimbatore, India  
Arad, Romania  
August 2018

Jude Hemanth  
Valentina Emilia Balas

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# Chapter 1

## Firefly Optimization Based Improved Fuzzy Clustering for CT/MR Image Segmentation



S. N. Kumar, A. Lenin Fred, H. Ajay Kumar  
and P. Sebastin Varghese

**Abstract** The segmentation is the process of extraction of the desired region of interest. In medical images, the anatomical organs and anomalies like a tumor, cysts, etc. are of importance for the diagnosis of diseases by physicians for tele-medicine applications. The thresholding, region growing, and edge detection are termed as classical segmentation algorithms. Clustering is an unsupervised learning technique to group similar data points and fuzzy partitioning merges similar pixels based on the fuzzy membership value. The classical FCM algorithm lacks sensitivity in the cluster centroid initialization and often gets trapped in local minima. The optimization algorithm gains its importance in cluster centroids initialization, thereby improving the efficiency of FCM algorithm. In this work, firefly optimization is coupled with FCM algorithm for CT/MR medical image segmentation. Fireflies are insects having a natural capacity to illumine in dark with glowing and flickering lights and firefly optimization algorithm was modeled based on its biological traits. The preprocessing stage comprises of artifacts removal and denoising by Nonlinear Tensor Diffusion (NLTD) filter. The computation time was minimized by reducing the total pixels count for the processing. The Firefly optimization, when coupled with FCM, generates satisfactory results inconsistent with FCM when coupled with Cuckoo, Artificial Bee Colony, and Simulated annealing algorithms. The cluster validity performance metrics are used for the determination of optimum number of clusters. The algorithms are developed in Matlab 2010a and tested on real-time abdomen datasets.

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**Keywords** Unsupervised learning • Clustering • Fuzzy C means  
FCM-firefly algorithm • FCM-artificial bee colony algorithm • FCM-cuckoo  
algorithm

## 1.1 Introduction

Medical image processing refers to the application of computer-aided algorithms for the extraction of anatomical organs and analysis of anomalies like a tumor, cyst, etc. The various steps in image processing are restoration, enhancement, segmentation, classification, and compression. The segmentation can be defined as the extraction of Region of Interest (ROI). The Computer Tomography (CT), Magnetic Resonance Imaging (MRI), Ultrasound and Positron Emission Tomography (PET) are the widely used medical imaging modalities for the disease diagnosis. The choice of segmentation algorithm depends on the medical imaging modality and its characteristics.

The CT images, in general, are corrupted by Gaussian noise and its distribution is as follows.

$$p(z) = \frac{1}{\sqrt{2\pi}\sigma} e^{-(x-\mu)^2/2\sigma^2}$$

where  $x$  represents random variable normally distributed with mean  $\mu$  and standard deviation  $\sigma$ .

The MR images are corrupted by rician noise, artifacts and intensity inhomogeneity due to the non-uniform response of RF coil. The rician noise distribution is as follows

$$p(z) = \frac{z}{\sigma^2} \exp\left(-\frac{z^2 + I^2}{2\sigma^2}\right) B\left(\frac{z\alpha}{\sigma^2}\right)$$

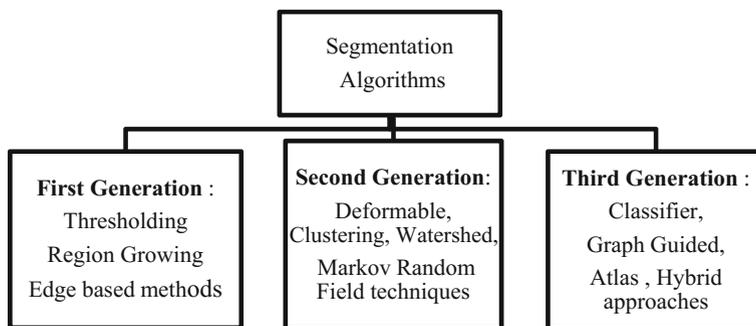
where,  $I$  is the true intensity value,  $\sigma$  is the standard deviation of the noise, and  $B$  is the modified zeroth order Bessel function.

The Ultrasound images, in general, are corrupted by speckle noise and its distribution is as follows.

$$F(x) = \left(\frac{g^{\gamma-1}}{(\gamma-1)!a^\gamma} e^{-\frac{x}{a}}\right)$$

where,  $\alpha$  is the variance,  $\gamma$  is the shape parameter of gamma distribution and  $g$  is the gray level.

Prior to segmentation, the preprocessing was performed by appropriate filtering technique; Filter selection is based on the medical imaging modality and noise characteristics. The role of preprocessing is inevitable in signal and image



**Fig. 1.1** Classification of segmentation algorithms

processing for subsequent operations like segmentation and classification [1, 2]. The segmentation algorithms can be categorized based on the generation of evolution and are depicted in Fig. 1.1.

Image segmentation is the process of grouping the pixels of an image to form meaningful regions. Medical image segmentation is the visualization of the region of interest such as anatomical structures and anomalies like tumor, cyst, etc. for medical applications such as diagnostics, therapeutic planning, and guidance. Lay Khoon Lee et al. performed a review on different types of segmentation algorithms for medical imaging modalities like X-ray, CT, MRI, 3D MRI and Ultrasound [3]. Similarly, S. N. Kumar et al. performed a detailed study on the different generation of the medical image segmentation techniques; qualitative and quantitative analysis was performed for the widely used medical image segmentation algorithms [4]. Neeraj Sharma et al. state the necessity of automated medical image segmentation technique in diagnosis, and radiotherapy planning in medical images and also explained the limitations of the existing segmentation algorithms [5]. The thresholding is a simple and classical technique that separates the foreground and background regions in an image based on the threshold value. The multilevel thresholding eliminates the discrepancy of the bi-level thresholding that uses a single threshold value. The optimization techniques when employed in the multilevel thresholding yield efficient results, since it provides the proper choice of threshold values. The 3D Otsu thresholding was found to be efficient for MR brain images; better results were produced than bi-level and multithresholding techniques [6]. Among the region based approaches, the classical region growing is the semi-automatic segmentation technique that relies on the seed point selection [6]. The multiple-seed point based region growing for brain segmentation was found to be effective on a multi-core CPU computer [7]. The manual seed point selection can be replaced by the deployment of the optimization algorithm for yielding efficient results [8]. The edge detection traces the boundary of objects in an image and among the classical edge detector, canny produces better results [9]. The Markov basics and Laplace filter were coupled to form an edge detection model that gives better results for medical images than the classical techniques [10]. The teaching

learning-based optimization was found to be effective for medical image edge detection than the classical edge detectors [11]. The interactive medical image segmentation algorithms are discussed in [12]. J. Senthilnath et al. did a performance study on nature-inspired firefly optimization algorithm in the thirteen benchmark classification datasets [13]. Superior results were produced when compared with classical techniques like Particle Swarm Optimization (PSO), Bayes net, Multilayer Perceptron, Radial Basis Function Neural Network, KStar, Bagging, MultiBoost, Naive Bayes Tree, Ripple Down Rule, Voting Feature Interval.

Iztok Fister et al. made a detailed analysis of the types of firefly algorithm for engineering applications in solving the real world challenges [14]. Hui Wang et al. proposed a modification in the parameter of classical firefly algorithm to reduce the complexity of the algorithm [15]. The proposed adaptive firefly algorithm generates better solution when compared with standard Firefly Algorithm, Variable step size Firefly Algorithm (VSSFA), Wise step strategy Firefly Algorithm (WSSFA), Memetic Firefly Algorithm (MFA), Firefly Algorithm with chaos and Firefly Algorithm with random attraction. Mutasem K et al. proposed a hybrid technique comprising of the Fuzzy C-Means algorithm with Firefly algorithm for the segmentation of brain tumor [16]. The experimental analysis was carried out on 181 brain images obtained from brain-web Simulated Brain Database (SBD) repository; robust results were produced when compared with Dynamic clustering algorithm based on the hybridization of Harmony Search and Fuzzy Variable String Length Genetic Point symmetry techniques. K. Vennila et al. proposed multilevel Otsu image segmentation based on Firefly optimization and good results were obtained in terms of PSNR, computation cost and mean value when compared with Darwinian Particle Swarm Optimization [17]. Cholavendhan Selvaraj et al. made a detailed survey of the bio-inspired optimization algorithms such as Ant Colony Optimization, Particle Swarm optimization, Artificial Bee Colony algorithm and their hybridizations [18].

The summarization of results reflects the status of the optimization techniques in solving the wide range of engineering problems. In the medical image processing, the FCM plays a major role in the clustering and classification of the image for the analysis, diagnosis, and recognition of anomalies [19]. Janmenjoy Nayak et al. performed a survey on major modification and advancement in the classical FCM algorithm and their applications towards the image analysis [20]. Chih Chin Lai et al. proposed a hierarchical evolutionary algorithm based on genetic algorithm for the segmentation of skull images which enhances the diagnostic efficiency than the dynamic thresholding, Competitive Hopfield Neural Networks (CHNN), K-Means and Fuzzy C-Means algorithms [21].

Emrah Hancer et al. proposed a methodology for the segmentation of brain tumor in the MRI images by using artificial bee colony algorithm. Efficient results were produced when compared with K-Means, FCM, and Genetic Algorithm based image segmentation techniques [22]. The FCM, when coupled with PSO was found to be effective for the segmentation of noisy images when compared with K-means, Enhanced FCM, and Fast Global Fuzzy Clustering techniques [23].

The Convolution Neural Network (CNN) was employed for the automatic segmentation of MR brain images, multiple convolution kernels of varying size was used for the generation of accurate results [24]. The CNN with multiple kernels of smaller size was used for the efficient brain tumor segmentation in MR images [25]. The Deep Learning Neural Network (DLNN) gains its importance in attenuation correction of PET/MR images [26]. The DLNN along with deformable model was proposed for the automatic segmentation of left ventricle in cardiac MR images [27]. The Deep Convolution Neural Network (DCNN) along with the 3D deformable model generates good segmentation results for the extraction of tissues in musculoskeletal MR images [28]. Vijay Badrinarayanan et al. proposed SegNet, a novel DCNN architecture for semantic pixel-wise segmentation [29]. In this chapter, firefly optimization algorithm was coupled with FCM for CT/MR medical image segmentation. The preprocessing stage comprises of artifacts removal and denoising by Non-Linear Tensor Diffusion (NLTD) filter. The computation complexity of the algorithm was minimized by sampling the total pixel count for manipulation. The Cluster Validity Indexes (CVI's) are used for the validation of results to determine the optimum number of clusters.

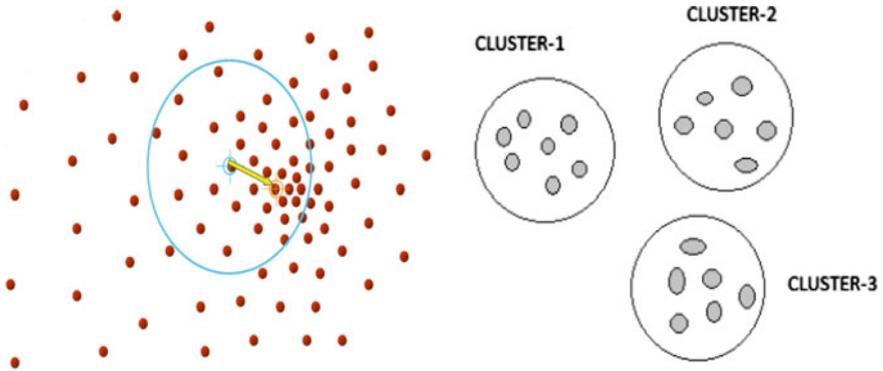
## 1.2 Materials and Methods

### 1.2.1 Data Acquisition

The real-time abdomen CT data sets are used in this work for the analysis of algorithms. The images are acquired from Optima CT machine with a slice thickness of 3 mm. The images in DICOM format with a size of  $512 \times 512$  are used in this work. The Metro Scans and Research Laboratory approved the study of human datasets for research purpose. The five abdomen CT data sets, each comprising of 200 slices are used in this work. The results of typical slice from each dataset are depicted here.

### 1.2.2 Fuzzy C Means Clustering

In this chapter, the Fuzzy c-means Clustering algorithm coupled with optimization technique was proposed for the segmentation of medical images. In the perspective of image processing, clustering is defined as the grouping of pixels into a cluster which is similar between them, while dissimilar pixels belong to other clusters. The concept of clustering is depicted below in Fig. 1.2. The clustering algorithms can be classified into two groups; Supervised and Unsupervised. The requirement of prior knowledge termed as training samples is the key concept of the supervised classifier. Artificial Neural Network (ANN), Naive Bayes Classifier, and Support



**Fig. 1.2** Principle of clustering

Vector Machine are some of the widely used supervised algorithms. The unsupervised technique doesn't need any prior information and is particularly well suited for huge unlabeled datasets. The unsupervised clustering techniques can be further classified into two categories; hierarchical and partitional. The role of partitional clustering is prominent in image analysis and pattern recognition. The K-means and Fuzzy c-means (FCM) are well-known partitional clustering algorithms. The K-means clustering is termed as Crisp (hard) since the objects are assigned to only one cluster. The FCM clustering is termed as soft (Fuzzy) since an object can be accommodated in more than one cluster based on the fuzzy membership value.

The FCM overcomes the issues of classical K-means clustering; since the data can belong to more than one cluster. The FCM was developed by Dunn [30] and modified by Hathaway and Bezdek [31] which was widely used for pattern classification. FCM is an unsupervised algorithm based on the minimization of the objective function.

$$J_m = \sum_{i=1}^N \sum_{j=1}^C U_{ij}^m \|y_i - c_j\|^2, \quad 1 \leq f < \infty$$

The pixels are grouped into clusters in such a manner that, the intracluster similarity is maximized and the intercluster similarity is minimized.

The fuzzy partition represents the fuzzy membership matrix of the pixel in the cluster. The parameter  $U_{ij}$  represents the fuzzy membership of the  $i$ th object (pixel) in the  $j$ th cluster. The parameter 'f' depicts weighting exponent that determines the degree of fuzziness for the fuzzy membership function. The fuzzy classification is based on the iterative optimization of the objective function depicted above with the updation of membership function  $u_{ij}$  and the cluster center  $c_j$  as follows.

$$U_{ij} = \frac{1}{\sum_{K=1}^C \left( \frac{\|y_i - c_j\|}{\|y_i - c_k\|} \right)^{\frac{2}{f-1}}}$$

$$c_j = \frac{\sum_{i=1}^N U_{ij}^f \cdot y_i}{\sum_{i=1}^N U_{ij}^f}$$

The iterative calculation is terminated, when  $\max_{ij} \{ |u_{ij}^{(k+1)} - u_{ij}^{(k)}| \} < \delta$ , where  $\delta$  is a termination criterion between 0 and 1, and  $k$  represents the iteration count. The convergence of the algorithm occurs when the objective function ( $J_m$ ) attains local minima or saddle point.

The steps in FCM clustering algorithm are summarized as follows

1. *Initialise*  $U = [U_{ij}]$  matrix,  $U^{(0)}$
2. *At*  $k^{\text{th}}$  *step*: Calculate the cluster center vector  $C^{(k)} = [c_j]$  with  $U^{(k)}$

$$c_j = \frac{\sum_{i=1}^M U_{ij}^m \cdot x_i}{\sum_{i=1}^M U_{ij}^m}$$

3. *Update*  $U^{(k)}, U^{(k+1)}$

$$U_{ij} = \frac{1}{\sum_{K=1}^C \left( \frac{\|x_i - c_j\|}{\|x_i - c_k\|} \right)^{\frac{2}{m-1}}}$$

4. *If*  $\|U^{(k+1)} - U^{(k)}\| < \delta$ , *then Stop*; *otherwise return to step 2.*

The operating principle of FCM is based on the fact that, the minimization of the objective function ends up with the solution. In many real-time cases, classical FCM stuck into local minima. The optimization algorithm can be employed to achieve global minima. The parameter selection is vital for optimization algorithms and it influences the performance of the algorithm to maximize or minimize the objective function subjecting to certain constraints. The cluster centers are randomly initialized by classical FCM, hence the optimization based clustering solves this problem. The cluster centers generated by the optimization technique is utilized by the FCM for image segmentation. The pixels in the image are mapped into the

particular cluster based on similarity and distance. The initialization of the cluster centers by optimization improves the performance in terms of the convergence rate, computation complexity, and segmentation accuracy.

### 1.2.3 Firefly Optimization Algorithm

In this chapter, the performance of firefly optimization in the FCM algorithm was analyzed for the estimation of optimal cluster center values for image segmentation. The biological trait of the firefly is the motivation for Yang [32] to propose an optimization technique. The rhythmic flashes generated by the firefly was used as a mode of communication between them to search for prey and for mating. More than 2000 species of fireflies are there in the world and they have natural characteristics to create illumination in the dark with flickering and glowing lights. Fister et al. found that the attraction capacity of the fireflies is proportional to the brightness [14]. The fireflies tend to move towards ones which emits a brighter light.

The population-based firefly algorithm was found to generate a global optimal solution for many engineering problems. The biological chemical substance luciferin present in the body of the fireflies was responsible for flashing the light. The intensity of light emitted is directly proportional to the discharge of luciferin. The degree of attraction tends to decrease as the distance between the fireflies increases. If any firefly fails to discover another firefly which is brighter than itself, it will travel arbitrarily. The optimization algorithm when employed for clustering applications, cluster centers are the decision variables and the objective function is associated with the euclidean distance. Based on the objective function, initially, all the fireflies will be spread randomly over the search space.

The two stages of firefly algorithm are summarized as follows:

The first stage is based on the difference in the intensity that is associated with the objective function values. Depending on the nature of the problem that requires maximization/minimization, a firefly with higher/lower intensity will entice another individual with higher/lower intensity.

Consider that there are  $n$  swarms (fireflies), where  $Y_i$  signifies the solution of a firefly  $i$ . The fitness value is expressed by  $f(Y_i)$  moreover the current position  $I$  of the fitness value  $f(y)$  is estimated by the brightness of a firefly [32].

$$I_i = f(y_i), \quad 1 \leq i \leq n$$

The second stage is the movement towards the firefly with high brightness intensity. The attraction factor of the firefly is represented by  $\beta$  that indicates the attraction power of firefly in the swarm and it changes with distance ( $R_{ij}$ ) between two fireflies  $i$  and  $j$  at positions  $Y_i$  and  $Y_j$  respectively.

$$R_{ij} = \|Y_i - Y_j\| = \sqrt{\sum_{k=1}^d (Y_{ik} - Y_{jk})^2}$$

The attraction function  $\beta(R)$  of the firefly is expressed as follows.

$$\beta(R) = \beta_0 e^{-\gamma R^2}$$

where  $\beta_0$  is the attraction function value for  $R = 0$ ,  $\gamma$  is the coefficient of ingestion of light.

The pseudo code for firefly optimization algorithm is as follows

```

Define objective function  $f(Y)$ ,  $Y=[Y_1, Y_2, Y_3, \dots, Y_d]$ 
Generate initial population of fireflies  $Y_i = [1, 2, 3, \dots, n]$ 
Estimate the light intensity of firefly  $I_i$  using the objective function  $f(Y)$ 
Define light absorption coefficient ( $\gamma$ )
While ( $t < \text{max generation}$ )
    for  $i=1:n$  //all n fireflies
        for  $j=1:n$  // all n fireflies
            if ( $I_j > I_i$ )
                Move firefly  $i$  towards  $j$  in  $d$  dimensions.
            end if
                // Attraction capacity changes with distance
                //Validate new solutions and update light intensity
        end for j
    end for i
Estimate the current best by ranking the fireflies
end while

```

The motion of a firefly ‘i’ from the position  $Y_i$  which is attracted towards another brighter firefly ‘j’ at position  $Y_j$  is expressed as follows

$$Y_i(t+1) = Y_i(t) + \beta(R)(Y_i - Y_j) + \alpha \left( rand - \frac{1}{2} \right)$$

$$Y_i(t+1) = Y_i(t) + \beta_0 e^{-\gamma R^2} (Y_i - Y_j) + \alpha \left( rand - \frac{1}{2} \right)$$

where  $\alpha$  depicts the maximum radius of the random step. The term  $rand$  represents randomization parameter uniformly distributed between 0 and 1.

There are two special cases

Case i:  $r = 0$ , then  $\beta = \beta_0 e^0 = \beta_0$ , The air is absolutely clear with no light dispersion. The fireflies can see each other; exploration and exploitation is out of balance.

Case ii:  $r = \infty$ , then  $\beta = I_0 e^{-\infty d^2} = 0$ , The air is foggy with extreme light dispersion. The fireflies can't see each other; exploration and exploitation is out of balance.

### 1.2.4 Improved FCM-Firefly Optimization Segmentation Algorithm

The FCM clustering algorithm proposed here comprises of two stages. In the first stage, firefly optimization is employed to determine the near-optimal cluster centers. In the second stage, the cluster centers are used for the initialization of FCM algorithm. The firefly optimization algorithm makes the clustering an effective tool for medical image segmentation by eliminating the problem of sticking at local minima. The firefly optimization is a swarm intelligence based algorithm and hence it mimics its advantages.

The solution vector is expressed as follows

$$S = \begin{pmatrix} V_1 & V_2 & V_3 \\ S_1, S_2, \dots, S_i \dots S_d & S_1, S_2, \dots, S_i \dots S_d & S_1, S_2, \dots, S_i \dots S_d \end{pmatrix}$$

where  $S_i$  represents characteristics in numerical form such that  $S_i \in S$ . The 'S' depicts the array representing pixel attribute. Each cluster center  $V_i$  is represented by d numerical features  $(S_1, S_2, \dots, S_d)$ . Each solution vector is of the size  $(c \times d)$ , where c indicates given number of clusters and d represents the features of the dataset.

For the delineation of anomalies like tumor or cyst or anatomical organs, each pixel in the image is mapped into the clustering sector. The cluster centers are randomly initialized from the image pixel gray values with the randomly initialized solution vector, the fitness value is determined by the objective function. The solution vector is then rearranged based on the decreasing order of the objective function value. The firefly optimization determines near optimal cluster centers thereby ensuring global minima for FCM algorithm and hence eliminates the

trapping at local minima. The improved FCM based on firefly optimization replaces the classical techniques of random initialization.

Prior to filtering, the medical image film artifacts are eliminated by a statistical technique coupled with convex hull computational geometry [33]. The threshold value determined by standard deviation technique was used for the binarization of input image. The binarized image was then subjected to connected component labeling for the elimination of patient details and technical information. The convex hull of the resultant image was multiplied with the original image for the generation of artifacts removed image. The preprocessing of input image was performed by Non-Linear Tensor Diffusion (NLTD) filter prior to segmentation [34]. The NLTD ensures good edge preservation since the smoothing is heterogeneous and non-noisy pixels are not disturbed.

The computation complexity was minimized by reducing the pixel count for the processing by segmentation algorithm.

$$Rp = randperm(L)$$

The parameter  $S_p$  represents the pixels taken for optimization, here in this work 50% of the total pixels are taken. The  $L$  represents the total pixel count of the image to be segmented and  $randperm$  function returns a row vector depicting a random permutation of the integers from 1 to  $n$ .

$$S_n = ceil(L * S_p)$$

The  $S_n$  represents the number of pixels selected for optimization and the function below represents the subset of pixels chosen for optimization process

$$X_2 = X(Rp(1 : S_n), :)$$

The optimization of the objective function relies on the brightness and movements of the firefly. The firefly algorithm starts by initializing the population of fireflies. The intensity of light emitted by the firefly estimates the movement of the fireflies. The algorithm works in the iterative fashion. The intensity of  $i$ th firefly is compared with the  $j$ th firefly as follows

*if*  $\beta(i) > \beta(j)$   
*firefly j move towards firefly i*  
*else*  
*firefly i move towards firefly j*

The incorporation of firefly algorithm has significantly improved the segmentation results. There were four stages of Improved FCM-Firefly segmentation algorithm.

- i. Initialization phase
- ii. Intensity calculation phase
- iii. Movement calculation phase
- iv. FCM algorithm phase.

The goal of incorporating firefly optimization in FCM is to minimize the objective function with a global minima value. The cluster centers represent the decision parameters to minimize the objective function. The initialization of the firefly population is as follows

$$y_{ij} = [y_{i1}, y_{i2}, \dots, y_{ij}, \dots, y_{id}] \quad 2 < j < C$$

Each firefly in the population is represented by using the above equation. Where  $y_{ij}$  represents the  $j$ th cluster centre.

The population of the fireflies are initialized and randomly distributed in search space. The position of firefly depicts the possible solution (centroids) for the clustering problem. In this phase, the parameter like  $\beta_0, \gamma, \alpha$  and maximization iteration are also initialized. Once the initialization process is over, the intensity of each firefly is determined by estimating the distance between the position of the firefly and the entire data in the dataset. The minimum distance value among the population with respect to data from the dataset is considered. The intensity value of each firefly is determined based on the sum of minimum distance with respect to the data from the dataset.

The expression for determination of intensity is as follows

$$\beta(\text{FF}_j) = \sum_{i=1}^n d_i$$

where FF represents firefly,  $d_i$  represents the minimum distance value for a particular firefly.

The brightness of the fireflies indicates the movement of the fireflies in the search space. The intensity of fireflies is compared to determine the new position. The difference in the brightness triggers the movement. The firefly optimization is employed in the FCM algorithm to enhance the clustering operation. The new position of the entire swarm of the fireflies is determined by the FCM operator based on the current intensity value.

The FCM-Firefly algorithm is carried out through the updation of the membership value  $u_{ij}$  and position of the firefly  $y_j$  using the below equations

$$U_{ij} = \frac{1}{\sum_{k=1}^s \left( \frac{\|y_i - f_j\|}{\|y_i - f_k\|} \right)^{2/f-1}}, \quad 1 \leq i \leq N$$

where  $U_{ij}$  depicts the degree of membership of  $y_i$  in the firefly  $j$ , degree of fuzziness  $f = 2$  and  $y_i$  is the data associated with the firefly under study.

$$F_j = \frac{\sum_{i=1}^N u_{ij}^m \cdot x_i}{\sum_{i=1}^N u_{ij}^m}$$

The  $F_j$  represents the solution after applying FCM in the firefly  $j$ .

The new position of Firefly is determined and the intensity value is updated. The fixed number of iterations will be provided and at the end of the iteration, the best solution was determined.

### 1.3 Results and Discussion

The algorithms are developed in Matlab 2010a and tested on CT abdomen data sets. The system specifications are as follows; Intel Core i3 processor of 3.30 GHz with 4 GB RAM. In the scenario of medical image segmentation, fixing the number of clusters is cumbersome, since it cannot be initialized roughly by viewing the image. The validation metrics are employed for the optimal cluster selection.

This is performed in 3 steps

- i. The parameters of clustering algorithm except the cluster number is fixed.
- ii. The cluster number is varied from an initial value of 2 to an upper limit (max). The data partition is carried out for each cluster number.
- iii. The cluster validity indexes are applied on the data partition obtained from the previous stage for evaluation. Based on the values of CVI's, the cluster number selection is done.

The terminologies used in the formulation of cluster validity function are as follows

$N$ : the count of data objects for clustering

$f$ : the fuzzifier factor that represents the level of cluster fuzziness

$u$ : the  $i$ th data object,  $1 \leq i \leq N$

$P$ : the number of clusters

$C_p$ : the  $p$ th cluster,  $1 \leq p \leq P$

$|C_p|$ : the count of data objects in the  $p$ -th cluster

$V_p$ : the centroid of the  $p$ -th cluster

$\|u - v\|$ : the distance between a pair of data objects

$\mu_{ip}$ : the membership degree of  $u_i$  corresponding to  $C_p$ .

The FCM algorithm is an iterative technique in which the pixels are grouped into a cluster based on the membership degree through the minimization of the objective function.

$$\sum_{i=1}^M \sum_{p=1}^P \mu_{ip}^f \|u_i - V_p\|^2, \quad f \geq 1$$

The number of the cluster is taken initially P and randomly P centroids are selected. The objective function represented above is optimized in an iterative fashion by the updation of  $\mu_{ip}$  and  $V_p$  as follows

$$\mu_{ip} = \frac{1}{\sum_{j=1}^P \left( \frac{\|u_i - v_p\|^2}{\|u_i - v_j\|^2} \right)^{\frac{2}{f-1}}}$$

$$V_p = \frac{\sum_{i=1}^N \mu_{ip}^f u_i}{\sum_{i=1}^N \mu_{ip}^f}$$

The iteration terminates when,  $\|U_{T+1} - U_T\| < \epsilon$ , where  $U_T = [\mu_{ip}]$  represents the matrix comprising of all  $\mu_{ik}$ 's. T is the number of iteration and  $\epsilon$  is a threshold specified by the user. The clustering validity metrics are used to estimate the quality of clustering result. The partition coefficient (PC) and partition entropy (PE) is based only on the membership values of fuzzy partition dataset. The criteria for optimum cluster number selection is the maximization of (PC) or minimum of PE. The issues in the performance metrics, PC or PE is that they do not consider the geometrical properties of the dataset.

Xie Beni's index (XBI) and Fukuyama's and Sugeno's index (FSI) are also widely used classical CVI's. XBI and FSI focus on the characteristics, compactness, and separation. The numerical part of the expression XBI in Table 1.1 represents the compactness of fuzzy partition, the denominator part represents the strength of separation between the cluster for optimal clustering. The value of XBI should be minimized for optimum cluster number selection. The expression for FSI in Table 1.1 comprises of two terms. The first term represents the compactness measure and the second term represents separation measure. Though FSI and XBI consider the inter-cluster information, geometrical properties are not considered.

The DB index was obtained by the mean of cluster similarities. For each cluster P, the similarity between P and all other clusters are determined. The term  $S_p$  is represented as follows

$$S_p = \frac{1}{|C_p|} \sum_{U_i \in C_p} \|U_i - V_p\|^2$$

**Table 1.1** Classical clustering validation metrics

Cluster validity index	Formula
Partition coefficient (PC) [35, 36]	$PC = \frac{1}{N} \sum_{p=1}^P \sum_{i=1}^N \mu_{ip}^2$
Partition entropy (PE) [35, 36]	$PE(K) = \frac{1}{N} \sum_{p=1}^P \sum_{i=1}^N \mu_{ip} \log_2(\mu_{ip})$
Xie and Beni index (XBI) [37]	$XBI(K) = \frac{\sum_{p=1}^P \sum_{i=1}^N \mu_{ip}^2 \ u_i - v_p\ ^2}{N \cdot \min_{i \neq j} \ v_i - v_j\ ^2}$
The Fukuyama and Sugeno Index (FSI) [37]	$FSI(K) = \sum_{p=1}^P \sum_{i=1}^N \mu_{ip}^f \ u_i - v_p\ ^2 - \sum_{p=1}^P \sum_{i=1}^N \mu_{ip}^f \ v_p - \hat{v}\ ^2$

**Table 1.2** Clustering validation metrics based on compactness and separation ratio

Cluster validity index	Formula
Calinski-Harabasz index (CHI) [38]	$CHI(K) = \frac{B_p}{P-1} / \frac{W_p}{N-P}$
Silhouette coefficient index (SCI) [38]	$SCI(P) = SC_1(P) - SC_2(P)$
Centroid similarity index (CSI) [38]	$CSI(K) = \frac{\sum_{p=1}^P \left( \frac{1}{ C_p } \left( \sum_{u_j \in C_p} \max_{u_i \in C_p} \ u_j - u_i\  \right) \right)}{\sum_{j=1}^P \min_{i \neq j} \ v_i - v_j\ }$
Davies Bouldin index (DBI) [38]	$DBI = \frac{1}{P} \sum_{p=1}^P \max \frac{S_j + S_p}{\ V_j - V_p\ }$
Partition coefficient and exponential separation index (PCAESI) [38]	$PCAESI = \sum_{p=1}^P \sum_{i=1}^N \frac{\mu_{ip}^2}{\mu_M} - \exp \left( \frac{-\min_{h \neq p} \ v_p - v_h\ ^2}{\beta_T} \right)$
Pakhira-Bandyopadhyay-Maulik index (PBMFI) [39]	$PBMFI = \frac{\max_{j \neq lp} \{ \ V_j - V_p\  \} \times \sum_{i=1}^N \mu_{il} \ U_i - V_l\ }{P \sum_{p=1}^P \sum_{i=1}^N \mu_{ik}^f \ U_i - V_k\ }$
WL index (WLI) [38]	$WLI = \sum_{p=1}^P \sum_{i=1}^N \frac{\mu_{ip}^2 \ U_i - V_p\ ^2}{\sum_{i=1}^N \mu_{ip}}$

Table 1.2 represents the clustering validity metrics based on compactness and separation ratio.

The shortcoming of the traditional CVI's is that they are focusing only on the distance between the cluster centroids. The classical clustering validity indexes were not found to be good for large cluster numbers.

The CS index is a function of the cluster diameter and the mean distance between the cluster centers. The PCAES index is a function of exponential separation component, and normalized partition coefficient.

The CH index is based on the mean between and within the sum of squares. The terms in the CH index are represented as follows

$$B_P = \sum_{p=1}^P |C_p| \|v_p - \bar{v}\|^2$$

$$W_P = \sum_{p=1}^P \sum_{U_i \in C_p} \|u_i - v_p\|^2$$

The SC index is based on the combination of two functions and evaluates the compactness-separation ratio. The terms in the SC index are represented as follows

$$SC_1(P) = \frac{\frac{1}{P} \sum_{p=1}^P \|v_p - \bar{v}\|^2}{\sum_{p=1}^P \left( \sum_{i=1}^N \mu_{ip}^m \|u_i - v_p\|^2 / \sum_{i=1}^N \mu_{ip} \right)}$$

$$SC_2(P) = \frac{\sum_{p=1}^{P-1} \sum_{j=p+1}^P \left( \sum_{i=1}^N \left( \min(\mu_{ip}, \mu_{ij})^2 \right) / n_{ij} \right)}{\left( \sum_{i=1}^N \max_{1 \leq p \leq P} \mu_{ip}^2 \right) / \left( \sum_{i=1}^N \max_{1 \leq p \leq P} \mu_{ip} \right)}$$

where  $SC_1$  is related with the geometric properties of data;  $SC_2$  is related with the membership degree properties.

The PBMF index is based on the compactness within clusters and a large separation between clusters. The WL index estimates the compactness of clusters by taking into account fuzzy weighted distance and the fuzzy cardinality of clusters. The five abdomen medical data sets are used for the analysis of algorithms. The cluster number was changed from  $P = 2$  to 6 and for each cluster number, 10 times the executions are done and the performance metrics are validated.

The expression for  $\mu_M$  and  $\beta_T$  in PCAES index are as follows

$$\mu_M = \min_{1 \leq p \leq P} \left\{ \sum_{i=1}^N \mu_{ip}^2 \right\}$$

$$\beta_T = \frac{1}{P} \sum_{p=1}^P \|V_p - \bar{V}\|^2$$

The performance metrics of the first run for the data set (ID1) is represented below in Table 1.3. Each cluster validity metric was represented with  $\pm$  sign, the “+” indicates that the CVI value should be high and “-” sign indicates that the CVI value should be low. The representative input images corresponding to data sets (ID1 to ID5) after the removal of artifacts are depicted in Fig. 1.3. Figure 1.4 represents the NLTD filtering result. Compared with classical filters like median filter, Gaussian filter, and bilateral filter, the NLTD filter generates efficient result. In the median filter, the noise-free pixels are also affected. The edge preservation is poor in Gaussian and bilateral filter. The performance of Anisotropic Diffusion Filter (ADF) was clearly stated in [40]. The NLTD filter is an improved version of ADF, thereby providing promising restoration results. The FCM results when