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Stefan Thiele

# Read-Out and Coherent Manipulation of an Isolated Nuclear Spin

Using a Single-Molecule Magnet  
Spin-Transistor



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Stefan Thiele

# Read-Out and Coherent Manipulation of an Isolated Nuclear Spin

Using a Single-Molecule Magnet  
Spin-Transistor

Doctoral Thesis accepted by  
the University of Grenoble, France



Springer

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# **Supervisor's Foreword**

It is with great pleasure and the highest enthusiasm that I write this foreword to Stefan Thiele's thesis, which reports his most exciting results. Its endeavor is driven by one of the most ambitious, technological goals of today's scientists: the realization of an operational quantum computer. In this regard, the basic building block is generally composed of a two-level quantum system, namely a quantum bit (or qubit). Such a quantum system must be fully controllable and measurable, which requires a connection to the macroscopic world. In this context, solid-state devices, which establish electrical interconnections to the qubit, are of high interest, mainly due to the variety of methods available for fabrication of complex and scalable architectures. Moreover, outstanding improvements in the control of the qubit dynamics have been achieved in the last years. Among the different solid-state concepts, spin-based devices are very attractive because they already exhibit relatively long coherence times. For this reason, electrons possessing a spin 1/2 are conventionally thought as the natural carriers of quantum information. However, the strong coupling to the environment makes it extremely difficult to maintain a stable entanglement. Alternative concepts propose the use of nuclear spins as building blocks for quantum computing, as they benefit from longer coherence times compared to electronic spins, because of a better isolation from the environment. But weak coupling comes at a price: the detection and manipulation of individual nuclear spins remain difficult tasks. In this context, the main objective of the Ph.D. of Stefan Thiele was to lay the foundation of a new field called molecular quantum spintronics, which combines the disciplines of spintronics, molecular electronics, and quantum information processing. In particular, the objective was to fabricate, characterize, and study molecular devices (molecular spin-transistor, molecular spin-valve and spin filter, molecular double-dot devices, carbon nanotube, nano-SQUIDs, etc.) in order to read and manipulate the spin states of the molecule and to perform basic quantum operations. The visionary concept of the project is underpinned by worldwide research on molecular magnetism and supramolecular chemistry, and in particular within the European Institute of Molecular Magnetism (<http://www.eimm.eu/>), and collaboration with

outstanding scientists in the close environment. For the project, we found the following funding: the main contributions came from the French Research Agency (ANR), the Contrat Plan Etat Région (CPER), the European Research Council (ERC), the Réseau Thématique de Recherche Avancé (RTRA), and the support from our institute. The Ph.D. of Stefan Thiele was funded by an ERC advanced grant. Among the most important results before Stefan Thiele's Ph.D., we showed the possibility of magnetic molecules to act as building blocks for the design of quantum spintronic devices and demonstrated the first important results in this new research area. For example, we have built a novel spin-valve device in which a nonmagnetic molecular quantum dot, consisting of a single-wall carbon nanotube contacted with nonmagnetic electrodes, is laterally coupled via supramolecular interactions to a TbPc<sub>2</sub> molecular magnet [Ph.D. of Matias Urdampilleta (2012)]. The localized magnetic moment of the SMM led to a magnetic field-dependent modulation of the conductance in the nanotube with magnetoresistance ratios of up to 300 % at low temperatures. We also provided the first experimental evidence for a strong spin–phonon coupling between a single-molecule spin and a carbon nanotube resonator [Ph.D. of Marc Ganzhorn (2013)]. Using a molecular spin-transistor, we achieved the electronic read-out of the nuclear spin of an individual metal atom embedded in a single-molecule magnet (SMM) [Ph.D. of Romain Vincent (2012)]. We could show very long spin lifetimes (several tens of seconds). Here, the Ph.D. of Stefan Thiele started with a completely new breakthrough. He proposed and demonstrated the possibility to perform quantum manipulation of a single nuclear spin by using an electrical field only. This has the advantage of reduced interferences with the device and less Joule heating of the sample. As an electric field is not able to interact with the spin directly, he used an intermediate quantum mechanical process, the so-called hyperfine Stark effect, to transform the electric field into an effective magnetic field. His project was designed to play a role of pathfinder in this—still largely unexplored—field. The main target concerned fundamental science, but applications in quantum electronics are expected in the long run.

Grenoble  
April 2015

Dr. Wolfgang Wernsdorfer  
Research Director

# Abstract

The realization of a functional quantum computer is one of the most ambitious, technological goals of today's scientists. Its basic building block is composed of a two-level quantum system, namely a quantum bit (or qubit). Among the other existing concepts, spin-based devices are very attractive because they benefit from the steady progress in nanofabrication and allow for the electrical read-out of the qubit state. In this context, nuclear spin-based devices exhibit additional gain of coherence time with respect to electron spin-based devices due to their better isolation from the environment. But weak coupling comes at a price: the detection and manipulation of individual nuclear spins remain challenging tasks.

Very good experimental conditions were important for the success of this project. Besides innovative radio frequency filter systems and very low noise amplifiers, I developed new chip carriers and compact vector magnets with the support of the engineering departments at the institute. Each part was optimized in order to improve the overall performance of the setup and evaluated in a quantitative manner.

The device itself, a nuclear spin qubit transistor, consisted of a TbPc<sub>2</sub> single-molecule magnet coupled to source, drain, and gate electrodes and enabled us to read out electrically the state of a single nuclear spin. Moreover, the process of measuring the spin did not alter or demolish its quantum state. Therefore, by sampling the spin states faster than the characteristic relaxation time, we could record the quantum trajectory of an isolated nuclear qubit. This experiment shed light on the relaxation time  $T_1$  of the nuclear spin and its dominating relaxation mechanism.

The coherent manipulation of the nuclear spin was performed by means of external electric fields instead of a magnetic field. This original idea has several advantages. Besides a tremendous reduction of Joule heating, electric fields allow for fast switching and spatially confined spin control. However, to couple the spin to an electric field, an intermediate quantum mechanical process is required. Such a process is the hyperfine interaction, which, if modified by an electric field, is also referred to as the hyperfine Stark effect. Using the effect, we performed coherent rotations of the nuclear spin and determined the dephasing time  $T_2^*$ . Moreover,

exploiting the static hyperfine Stark effect we were able to tune the nuclear qubit in and out of resonance by means of the gate voltage. This could be used to establish the control of entanglement between different nuclear qubits.

In summary, we demonstrated the first single-molecule magnet based quantum bit and thus extended the potential of molecular spintronics beyond classical data storage. The great versatility of magnetic molecules holds a lot of promises for a variety of future applications and, maybe one day, culminates in a molecular quantum computer.

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Stefan Thiele

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# Chapter 1

## Introduction

### 1.1 Molecular Spintronics

The computer industry developed in the course of the last 60 years from its very infancy to one of the biggest global markets. This tremendous evolution was triggered by several historical milestones. In 1947, John Bardeen and Walter Brattain presented the world's first transistor [1] based on Walter Shockley's field-effect theory. Their discovery was soon after rewarded by the Nobel Prize in physics and led to the development of today's semiconductor industry.

Another groundbreaking discovery was made in 1977, when Alan Heeger, Hideki Shirakawa, and Alan MacDiarmid presented the first conducting polymer [2]. Their work opened the way for organic semiconductors, which stand for cheap and flexible electronics like organic LEDs, photovoltaic cells, and field-effect transistors. With still a lot of ongoing fundamental research, some fields already reached maturity. Especially, organic LEDs became an irreplaceable part of modern televisions in the last couple of years. The major impact of organic semiconductors was awarded by Royal Swedish Academy of Sciences with the Nobel Price in chemistry.

On decade later, in 1988, Peter Grünberg and Albert Fert reported an effect, which they called the giant magneto resistance (GMR) [3, 4]. In contrary to conventional electronic devices, which use charges as carriers of information, the GMR exploits the electronic spin degree of freedom. Their discovery led to the development of a completely new branch of research, which is these days referred to as spintronics. With the success of data-storage industry, in the last 25 years, devices using the GMR effect became a part of our everyday live.

The drive for steady innovation led researchers to think about new devices which unify these great ideas and would, therefore, be even more performing. The famous article of Datta and Das in 1990 [5] was the first step towards a new age of spintronic devices. Their proposal described a transistor, which could amplify signals using spins currents only. However, for this transistor to work, efficient spin-polarization, injection, and long relaxation times are necessary. Especially, the relaxation time is usually limited by spin-orbit coupling and the hyperfine interaction.