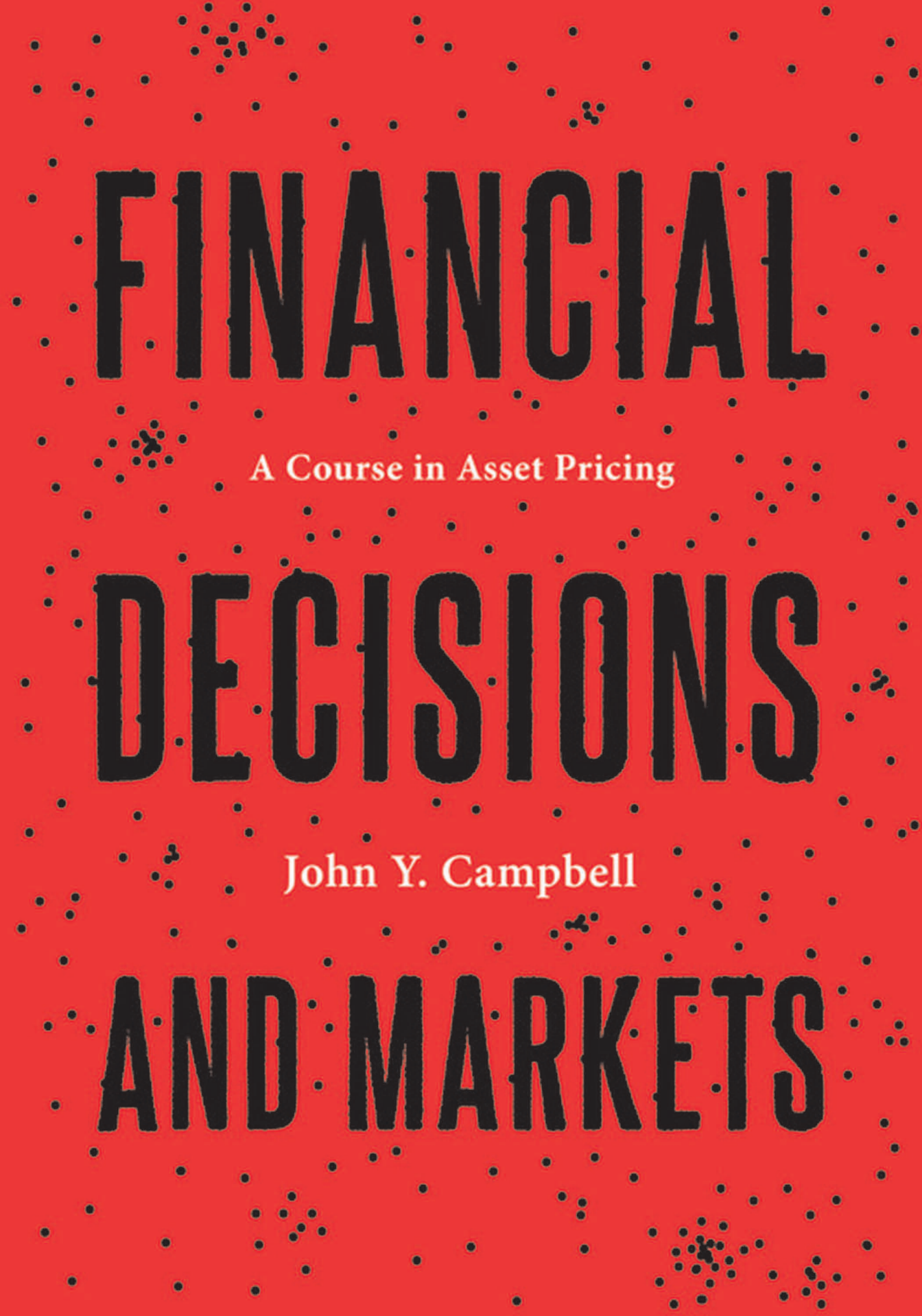




**FINANCIAL**

A Course in Asset Pricing

**DECISIONS**

John Y. Campbell

**AND MARKETS**





# Financial Decisions and Markets: A Course in Asset Pricing

**John Y. Campbell**

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*To Graham, Malcolm, Naomi, and Sophia*



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